Water-solubility-driven separation of gases using graphene membrane

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1. Introduction

Separation of CO\textsubscript{2} from the flue gas is an important step towards reducing the global emissions of CO\textsubscript{2}. Many processes such as adsorption, absorption and membrane technology have been used to remove CO\textsubscript{2} from the flue gas [1,2]. A popular industrial method to separate CO\textsubscript{2} is to use amine solvents in the absorption process. In spite of high product yields and purities, high energy consumption and liquid loss in desorption are regarded as disadvantages of the approach [2,3]. On the other hand, membrane technology has been considered as an energy efficient method for CO\textsubscript{2} separation for a couple of decades, as membranes are thin and easy to scale-up [4]. Recent studies on gas separation through membranes have focused on inorganic membranes such as zeolites and carbon-based membranes for high-temperature environments [5–8]. The thickness of these membranes ranges from tens of nanometers to several micrometers.

Taking advantage of both the absorption and the membrane technologies, a couple of methods have been proposed. The first one is a membrane contactor in which a membrane acts as an interface between the feed gas and the absorption liquid [9,10]. CO\textsubscript{2} is solvated in the absorption liquid through the membrane and this solvated CO\textsubscript{2} is separated later by using stripper or the same type of membrane contactor called desorber [11]. The second approach uses a liquid membrane, where an absorption liquid and polymeric membranes are placed between two gas regions. CO\textsubscript{2} in the feed gas region penetrates through the liquid membrane and comes out to the other region [12]. Ever since the liquid membrane (or membrane contactor) was introduced [13,14], separation methods based on the absorption liquid and the membrane have improved over a couple of decades and researchers have primarily focused on various systems and diverse materials in the liquid membrane system. To achieve efficient gas separation through the liquid membrane, the type of absorption liquid used in the system is important. Water as an absorption liquid has steadily received much attention for gas separation [11,15,16]. In addition, different materials for the membrane have been used instead of the conventional polymeric membrane, to reduce the overall diffusion thickness.

Graphene is a promising material for various applications because of its exceptional physical properties and atomic scale thickness [17]. Graphene is a single-atom-thick planar sheet made of carbon atoms arranged in a hexagonal lattice. Graphene, without defects, does not have pores and is impermeable, but atomic scale pores can be generated in a graphene sheet by chemical or thermal treatment [18,19]. Porous graphene has been investigated as a membrane material and it has been shown to be a fast transporter of water [20]. In addition, porous graphene has also been shown to be a high performance membrane material for ion, gas and nanoparticle separation [21–23]. Jiang et al. considered graphene with subnanometer size pores as a membrane for gas separation and observed that porous graphene can be a highly efficient membrane for gas separations [22].

In this paper, we investigate water solubility-driven separation of CO\textsubscript{2} from CO\textsubscript{2}/O\textsubscript{2}, CO\textsubscript{2}/N\textsubscript{2} and CO\textsubscript{2}/CH\textsubscript{4} mixtures using a porous graphene membrane. Molecular dynamics simulation is an important tool to understand the vapor–liquid and liquid–solid interface effects on the separation procedure and the coupled interaction of gas with the graphene pore and the water slab [24].
By performing extensive molecular dynamics simulations, we understand separation of gases. To investigate the merits of porous graphene for gas separations, we also perform molecular simulations using carbon nanotubes (CNT). Studies on CNT have shown fast transport of water and gases through the tubes [25–27], so comparison studies between porous graphene and CNT can provide insights on the effect of the length of the pore on gas separations. We envision that our work will lead to the use of porous graphene as an efficient membrane for gas separations.

### 2. Methods

We performed molecular dynamics simulations to investigate water solubility-driven separation of gases through a porous graphene membrane. A snapshot of the CO$_2$/O$_2$ mixture and the water slab separating the mixture and the porous graphene membrane is shown in Fig. 1(a). The volume of the system (3.9 x 3.8 x 14.0 nm$^3$) is fixed throughout the simulation. The gas mixture is initially positioned at both ends of the system. During simulation, the gas molecules penetrate through the water slab and the porous graphene membrane and enter into the middle region, which is initially empty. The 0.99 nm diameter graphene pore is shown in Fig. 1(b). The thickness of the water slab is approximately 2.4 nm. The bond length of CO$_2$, O$_2$, and N$_2$ is maintained by the shake constraint scheme. The bond stretching and angle bending of CH$_4$ is controlled by the OPLS-AA force field [28]. The non-bonded potential energy between molecules is given by

$$E_{\text{nonbond}} = E_{ij} + E_{\text{Coulomb}}$$

where

$$E_{ij} = \sum_{i<j} 4\epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{6} \right]$$

$$E_{\text{Coulomb}} = \sum_{i<j} q_i q_j \frac{q_i q_j}{r_{ij}}$$

The Lennard–Jones (L–J) and Coulomb potential parameters for the various gas molecules (CO$_2$, O$_2$, N$_2$, and CH$_4$) are taken from [28–30]. We estimated the solubility of CO$_2$ [29,31,32], O$_2$ [30,33,34], N$_2$ [29,30,33] and CH$_4$ [28,35] by the method discussed in Ref. [36] using SPC/E water slab at 300 K. The models used in this work for CO$_2$, O$_2$, N$_2$, and CH$_4$ show the closest solubility of each gas in water to experimental data at 300 K. For water, SPC/E model is used [37]. The porous graphene membranes are positioned at $z=5$ nm and $z=9$ nm. The force-field parameters for the carbon atom of the graphene membrane are taken from [38]. The L–J parameters between different molecules were obtained by applying the Lorentz–Berthelot mixing rules, $\sigma_{ij} = (\sigma_i + \sigma_j)/2$ and $\epsilon_{ij} = \sqrt{\epsilon_i \epsilon_j}$. A cut-off distance of 1.2 nm is used for the L–J potential. Electrostatic interactions were computed by using the Particle Mesh Ewald method with a grid spacing of 0.15 nm. Periodic boundary conditions are applied in all three directions. Time integration was performed by using the leap-frog algorithm with a time step of 1.0 fs. The temperature of the system is maintained at 300 K by Nose–Hoover thermodinamics with a characteristic time of 0.1 ps [39]. Simulations were performed using GROMACS 4.0.7 [40].

### 3. Results and discussion

#### 3.1. Solubility of gases in water

Before presenting results on the separation of gases through the porous graphene membrane, we discuss the solubility of the various gases considered in this work (CO$_2$, O$_2$, N$_2$, and CH$_4$) in bulk water at 300 K. The solubility results will not only explain the separation properties, but also show the limitations, if any, of the force-fields in accurately representing experimental solubility data. We estimated the solubility of each gas using the method discussed in [36]. We simulated the water slab system, as shown in Fig. 2(a), with 98 gas molecules and 1600 water molecules at 300 K. Using the averaged value of gas concentration along the z-axis, as shown in Fig. 2(b), we calculated gas concentration in the water slab. Since the concentration of gas in water is proportional to gas vapor pressure, we can compare the gas solubility by calculating the Henry’s constant (pressure unit) as shown in Table 1. The gas vapor pressure is calculated by van der Waals equation and Henry’s constant is calculated based on Henry’s law $h_i = p/x_i$, where $p$ is the pressure of gas in the vapor region and $x$ is the mole fraction of gas in the water slab. If the gas molecule has a smaller Henry’s constant, then it has a higher solubility. We note that CO$_2$ has higher solubility compared to that of N$_2$ and CH$_4$. The solubility of O$_2$ is about two times bigger than that of N$_2$ and the solubility of CH$_4$ is between that of O$_2$ and N$_2$. Even though there is some discrepancy between experimental solubilities and our estimated values, the ratios of various gas solubilities are reasonable compared to the experimental values and we will use this to explain gas separations.

#### 3.2. Separation of gas mixtures

As shown in Fig. 1(a), the computational domain for gas separations is divided into inside and outside regions. The separation of gas molecules is identified by the number of the gas molecules in the inside and outside regions as a function of the simulation time. Initially, the gas mixtures are positioned in the outside region, next to the water slab. The gas molecules diffuse through the water slab and through the porous graphene membrane to the inside region. To demonstrate the significance
of solubility-driven separation of gases, we also simulated graphene-only case, where the system setup is similar to Fig. 1, except that the water slab is not present.

The simulation results for the CO2/O2 mixture are shown in Fig. 3, for the CO2/N2 mixture in Fig. 4, and for the CO2/CH4 mixture in Fig. 5. The separation of gases in the absence of the water slab are also shown in these figures. In the case of graphene-only simulations (no water slab), equilibration is achieved within 3 ns and the number of gas molecules in the inside and the outside regions fluctuate around a fairly constant value. In the absence of the water slab, we note that for the various gas mixtures, the other gas molecule (O2, N2 and CH4) passes through the graphene nanopore slightly faster than the CO2 molecule. In this case, the size of the gas molecule relative to the size of the nanopore is important for gas selectivity. In the case of a 0.99 nm diameter graphene pore without the water slab, no significant selectivity or separation of the gas molecules is achieved for the various gas mixtures considered. Compared to the graphene-only case, in the presence of a water slab, as shown in Figs. 3(b), 4(b), and 5(b), a significant separation of gas molecules is observed. In particular, we observed that highly soluble CO2 molecules are selectively transported through the water/graphene membrane and other gas molecules such as O2, N2 and CH4 having low solubility in water hardly penetrate through the water/graphene membrane.

The flux of each gas molecule and the selectivity of CO2/O2, CO2/N2 and CO2/CH4 gas mixtures through the water/graphene membrane system are shown in Table 2. In the CO2/O2 case, the flux of CO2 is about 9.5 times higher than the flux of O2. The flux of N2 in the CO2/N2 mixture is lower than the flux of O2 in the CO2/O2 mixture and this reduction of N2 flux through the water/graphene membrane causes higher selectivity of CO2 for the CO2/N2 mixture than CO2 from the CO2/O2 mixture. Higher CO2 selectivity in the CO2/N2 mixture is consistent with the higher solubility ratio of CO2/N2 compared to that of CO2/O2. In the case of CO2/CH4 mixture, the selectivity of CO2 over CH4 is in between the selectivity of CO2 over N2 and CO2 over O2. This selectivity of CO2 from different gas mixtures can be explained by the solubility difference between CO2 and the other gas molecule (O2, N2 and CH4).

The water slab shown in Fig. 1(a) has two interfaces – vapor/water free interface and the water/graphene interface. Once the gas molecules (mainly CO2) dissolve in water from the vapor/water interface and pass through the graphene pore to the inside region of the system, they hardly penetrate back to the water slab through the graphene nanopore. This asymmetrical structure of the water/graphene membrane is useful to induce one-directional flux of gas molecules.

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We also increased the thickness of the water slab from 2.4 nm to 4.2 nm to investigate the effect of water thickness on selectivity. We repeated the simulation of CO$_2$/O$_2$ mixture using 4.2 nm water/graphene membrane system. The number of gas molecules in different regions of the system is shown in Fig. 6 (b). The flux of both CO$_2$ and O$_2$ molecules is smaller than in the 2.4 nm water slab case; the flux of CO$_2$ molecules is about 2.7 ns$^{-1}$ and the flux of O$_2$ molecules is about 0.21 ns$^{-1}$. The increased water slab thickness suppresses the flux of O$_2$ more than the flux of CO$_2$ which gives a higher selectivity of about 12.8 compared to 9.5 in the 2.4 nm water/graphene case. As the gas molecules do not penetrate through the thinner water slab easily compared to the thicker water slab and the concentration ratio in water is decided by the solubility, the gas flux through the thicker water slab approaches the solubility ratio between CO$_2$ and O$_2$ of 28.7.

During the simulations, no water molecules passed through the graphene pore. This can be explained by the strong interaction between water molecules, which is represented by the hydrogen bonding network. The strong water–water interaction and the relatively smaller interaction with graphene makes the penetration of water molecules through the nonpolar graphene pore difficult [41,42]. However, there is still a chance of water evaporating slowly from the system and water loss could be compensated by a refilling process through the $x$, $y$-directions. To prevent evaporation of the water slab in the water/graphene membrane, another membrane can be used at the free surface of the water slab. For example, a graphene membrane with a larger pore can be used. As shown in Fig. 7, we can see that the number of gas molecules in the reservoirs is maintained even after 30 ns.

### Table 2

<table>
<thead>
<tr>
<th>Gas mixture</th>
<th>CO$_2$ flux (# of molecules/ns)</th>
<th>Other gas flux (# of molecules/ns)</th>
<th>Selectivity</th>
</tr>
</thead>
<tbody>
<tr>
<td>CO$_2$/O$_2$</td>
<td>$4.1 \pm 0.3$</td>
<td>$0.43 \pm 0.04$</td>
<td>$9.5 \pm 0.7$</td>
</tr>
<tr>
<td>CO$_2$/N$_2$</td>
<td>$3.3 \pm 0.5$</td>
<td>$0.23 \pm 0.06$</td>
<td>$14.4 \pm 1.4$</td>
</tr>
<tr>
<td>CO$_2$/CH$_4$</td>
<td>$4.1 \pm 0.5$</td>
<td>$0.35 \pm 0.12$</td>
<td>$9.9 \pm 0.7$</td>
</tr>
</tbody>
</table>
A graphene membrane with a larger opening is used at the water/vapor interface to prevent evaporation of water and the inside graphene membrane has a pore of 0.99 nm pore. We investigated separation of the CO$_2$/$O_2$ mixture using the system shown in Fig. 7 and compared the results with the previous results. We observed that the separation of CO$_2$ was not as efficient as in the previous case as shown in Fig. 7(b). However, if we reduce the Lennard-Jones interaction parameter, $\epsilon$, of the outside graphene membrane to

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**Fig. 6.** Gas separation of CO$_2$/O$_2$ mixture with different thickness of water: (a) number of CO$_2$/O$_2$ in inside and outside through 2.4 nm water/graphene membrane; (b) number of CO$_2$/O$_2$ in inside and outside through 4.2 nm water/graphene membrane.

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**Fig. 7.** Gas separation of CO$_2$/O$_2$ mixture using a different water/graphene membrane: (a) snapshot of the system; (b) number of CO$_2$/O$_2$ molecules in inside and outside regions of the system; (c) number of CO$_2$/O$_2$ molecules in inside and outside regions with a reduced $\epsilon$. 
The excess chemical potential is an average over all the configurations. Defined as

\[ \mu_{ex} = kT \ln \langle V \int d\mathbf{s}_{N+1} \exp(-\beta \Delta U) \rangle / \langle V \rangle \]

(4)

where \( k \) is the Boltzmann constant, \( T \) is the temperature of the system, \( \beta = 1/kT \), \( V \) is the volume of the system, and \( \langle \ldots \rangle \) indicates an average over all the configurations.

The calculated excess chemical potential variation along the z-axis is shown in Fig. 8(b) and the average chemical potential value of each gas molecule in the water slab region is shown in Table 3. The potential difference of various gas molecules in the water slab region is reasonable and consistent with the solubility difference of gas molecules in water [45]. The chemical potential variation shows that the solubility difference in the water slab drives the selectivity of CO2 from CO2/O2, CO2/N2, and CO2/CH4 mixtures. In particular, when the gas molecules are near the porous graphene, the chemical potential difference between CO2 and other gases becomes smaller but still the difference is maintained which can be regarded as a combined effect of water and porous graphene.

3.4. Separations using CNT

To further understand the significance of separations using graphene, we performed gas separations using a carbon nanotube (CNT) and compared its performance with that of graphene. We considered a (13,0) CNT which has a diameter of 1.02 nm (this diameter is similar to the graphene nanopore size of 0.99 nm) and a length of 3 nm. Using the CNT structure as the membrane between vapor and water slab, we performed the simulation on CO2/O2 mixture to investigate gas selectivity difference between CNT and graphene pore. Other simulation conditions are identical to the graphene/water slab simulations. The system is again divided into inside and outside regions in CNT/water slab system and the CO2/O2 mixture is initially positioned in the outside region as shown in Fig. 9(a). We count the number of CO2 molecules in both the regions to estimate the separation of CO2 through the water/CNT membrane system (see Fig. 9(b) and (c)). As the CO2 molecules enter the CNT from the water slab, they fill the CNT. After a certain amount of CO2 molecules occupied the CNT (at around \( t = 10 \) ns), CO2 molecules begin to pass through the CNT and enter the inside region. The number of CO2 molecules in the CNT increase gradually until the CNT is completely filled with gas molecules. Once the CNT is completely filled at around \( t = 18 \) ns, the instant flux of the CO2 molecules passing through the water/CNT membrane reduces from 2.5 to 1.3 \( \text{nm}^{-1} \). CO2 filling the CNT reduces the flux of the gas molecules.

To understand this CO2 behavior, we calculate the interaction energy of various gas molecules with graphene and CNT when the gas molecule is in the middle of the membrane as shown in Fig. 10. Though CO2 interaction is stronger than O2, N2, or CH4 in both CNT and graphene structures, the interaction energy difference between CO2 and other gas molecules (O2, N2, and CH4) is larger in CNT than in the graphene pore as shown in Table 4. The strong interaction energy between CO2 and CNT makes the interior of the CNT a favorable place for CO2. Therefore, CO2 molecules are not able to escape easily until high density of CO2 in the CNT is achieved. The strong interaction between CO2 and CNT was also reported in Refs. [46,47]. The selectivity ratio of CO2 over O2 in the CNT/water slab system is about 7.5 (before filling) and about 3.3 (after filling), which is lower than the selectivity ratio of about 9.5 obtained in the graphene/water slab system. These results indicate that water solubility-driven separation of gases can be observed even in the case of CNT pores, but the length of the pore affects the separation ratio and graphene, because of its single-atom thickness, is ideally suited for water solubility-driven separation of gases. For the separation of other mixtures, CO2/CH4 and CO2/N2, we performed additional simulations and observed similar gas separation behavior.

4. Conclusions

We have shown that a graphene membrane can efficiently separate CO2 from CO2/O2, CO2/N2, and CO2/CH4 mixtures.
The separation ratio follows the water-solubility of the gas molecules in the mixture. By investigating the gas mixtures with and without water slab, we have shown that the separation of the gas mixtures can be controlled and the selectivity ratio can be enhanced with the water slab. A thicker water slab, provided a higher selectivity ratio. Even though carbon nanotubes have been shown to be fast transporters of gas and water molecules, we have shown that the graphene membrane, because of its single-atom thick

![Fig. 9. Gas separation of CO₂/O₂ mixture through water/CNT membrane: (a) snapshot of the system; (b) number of CO₂/O₂ in inside and outside regions; (c) number of CO₂/O₂ molecules in the CNT.](image)

![Fig. 10. Configuration for calculation of the interaction energy between a gas molecule and CNT/graphene: (a) configuration of CO₂ in a (13,0) CNT; (b) configuration of CO₂ in the graphene pore.](image)

<table>
<thead>
<tr>
<th>Gas</th>
<th>(13,0) CNT (kJ/mol)</th>
<th>Graphene pore (kJ/mol)</th>
</tr>
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<tbody>
<tr>
<td>CO₂</td>
<td>−31.2 ± 2.3</td>
<td>−9.6 ± 1.3</td>
</tr>
<tr>
<td>O₂</td>
<td>−16.4 ± 1.7</td>
<td>−5.1 ± 1.2</td>
</tr>
<tr>
<td>N₂</td>
<td>−19.4 ± 1.5</td>
<td>−6.2 ± 1.1</td>
</tr>
<tr>
<td>CH₄</td>
<td>−20.8 ± 1.8</td>
<td>−6.5 ± 1.3</td>
</tr>
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</table>
length compared to the finite length of the carbon nanotube, provides higher selectivity and faster transport of gas molecules compared to the carbon nanotube.

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References